

# A Drag-and-Drop Proof Tactic

Pablo Donato, Pierre-Yves Strub and Benjamin Werner

LIX, Ecole polytechnique, France

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# Disclaimers !

- ▶ This is *ongoing* work
  - ⇒ About the *interface*
- ▶ Education : prime goal
  - (possibly more applications later)

- ▶ Basic idea : in propositional calculus
- ▶ The rules
- ▶ Quantifiers / predicate calculus

$$[ \underline{A \Rightarrow B} \text{ } \textcircled{\vdash} \text{ } C \vee (D \wedge \underline{B}) ]$$

▼  $R_{\vee_2}$

$$C \vee [ A \Rightarrow B \text{ } \vdash \text{ } (D \wedge B) ]$$

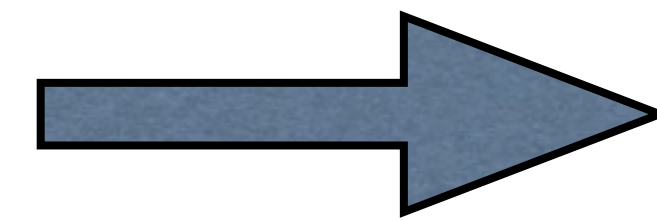
▼

$$C \vee (D \wedge [ A \Rightarrow B \text{ } \vdash \text{ } B ])$$

▼

$$C \vee (D \wedge A \wedge \textcircled{B \vdash B}) \quad \blacktriangleright$$

$$C \vee (D \wedge A \wedge T) \quad \blacktriangleright \quad C \vee (D \wedge A)$$



$$C \vee (D \wedge A)$$

deep inference  
(Calculus of Structures :  
see K. Chaudhuri's CADE talk)

Our set of rules  
subsumes all the  
given examples

# Conclusions

<https://prover.dioxygen.io/>

- ▶ Prototype : Actema - runs in JavaScript  
*Continuation of Proof-by-pointing*
- ▶ Started as very practical effort, but fruitful links with proof theory

## Possible future work

- ▶ Scaling up : add on a real theorem prover
- ▶ How to deal with lemmas and proof libraries, "Replay proofs"...
- ▶ Use of more complex actions (multi-touch...)
- ▶ Proof-theoretical properties (which forms of completeness...)
- ▶ Extending to classical logic, Higher-Order Logic, Type Theories